

1. What is the Pythagorean identity?

$$\underline{\cos^2 \theta + \sin^2 \theta = 1}$$

2. Use the Pythagorean identity to derive two other fundamental identities. Make sure to show your work.

$$\begin{aligned} \overbrace{\cos^2 \theta} + \overbrace{\sin^2 \theta} &= \overbrace{1} \\ \cos^2 \theta &= \overbrace{1} - \overbrace{\sin^2 \theta} \\ 1 &= \overbrace{\cos^2 \theta} + \overbrace{\sin^2 \theta} \\ 1 + \tan^2 \theta &= \sec^2 \theta \end{aligned}$$

$$\begin{aligned} \overbrace{\cos^2 \theta} + \overbrace{\sin^2 \theta} &= \overbrace{1} \\ \overbrace{\cos^2 \theta} &= \overbrace{1} - \overbrace{\sin^2 \theta} \\ \cot^2 \theta + 1 &= \csc^2 \theta \end{aligned}$$

3. Name all of the even/odd identities for the trig functions:

$$\sin(-\theta) = -\sin \theta$$

$$\csc(-\theta) = -\csc \theta$$

$$\cos(-\theta) = \cos \theta$$

$$\sec(-\theta) = \sec \theta$$

$$\tan(-\theta) = -\tan \theta$$

$$\cot(-\theta) = -\cot \theta$$

4. Write down the 3 periodic identities:  $\sin(\theta \pm 2n\pi) =$ 

$$\cos(\theta \pm 2n\pi) =$$

$$\tan(\theta \pm n\pi) =$$

Use your Trigonometric identities to find the value of the following:

5.  $\sin^2 40^\circ + \frac{1}{\sec^2 40^\circ}$

$$\sin^2 40 + \cos^2 40 = 1$$

6.  $\sec 55^\circ \cos 55^\circ$

$$\frac{1}{\cos 55} \cdot \cos 55 = 1$$

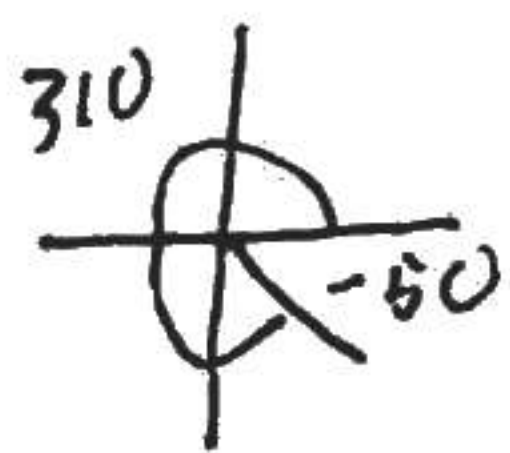
$$7. \frac{\cos(-40^\circ)}{\cos 40^\circ} = 1$$

$$\frac{\cos 40}{\cos 40}$$

$$8. \frac{\sin(-40^\circ)}{\sin 40^\circ} = -1$$

$$\frac{-\sin 40}{\sin 40}$$

$$9. \sin 310^\circ \csc(-50^\circ) = 1$$



$$\sin(-50) \cdot \frac{1}{\sin -50}$$

$$-\sin 50 \cdot \frac{1}{-\sin 50}$$

$$11. \cot^2 \theta - \csc^2 \theta + 1 = 0$$

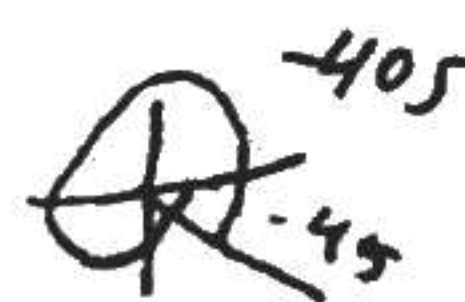
$$\cot^2 \theta + 1 - \csc^2 \theta$$

$$= \csc^2 \theta - \csc^2 \theta$$

$$10. \overset{\cos 180}{\cos(540^\circ)} - \tan(-405^\circ)$$

$$-1 + 1 =$$

$$0$$



$$12. \tan^2 \theta - 1 - \frac{1}{\cos^2 \theta}$$

$$-2$$

$$\tan^2 \theta - 1 - (\sec^2 \theta)$$

$$\tan^2 \theta - 1 - (1 + \tan^2 \theta)$$

$$\tan^2 \theta - 1 - 1 - \tan^2 \theta$$

$$-2$$