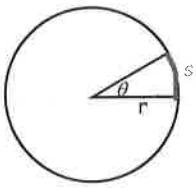


wk3_d4.notebook

Arc Length of a Circle: s denotes the length of the arc of a circle of radius r subtended by the central angle θ



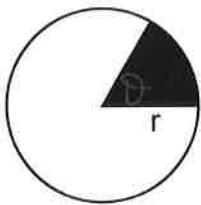
$$C = 2\pi r$$

In degrees: $s = \frac{\theta}{360} \cdot 2\pi r = \frac{\pi r \theta}{180}$

In radians: $s = \frac{\theta}{2\pi} \cdot 2\pi r = r\theta$

So, if the angle is in radians, the length of the arc, s , is found with the formula: $s = r\theta$

Area of a sector:



$$A = \pi r^2$$

In degrees: $A = \frac{\theta}{360} \cdot \pi r^2$

In radians: $A = \frac{\theta}{2\pi} \cdot \pi r^2 = \frac{1}{2} r^2 \theta$

So, if the angle is in radians, the area of the sector is given by the formula: $A = \frac{1}{2} r^2 \theta$

s denotes the length of the arc of a circle of radius r subtended by the central angle θ . Find the missing quantity. Round answers to three decimal places.

1. $r = 20$ meters, $\theta = \frac{1}{3}$ radian, $s = ?$

part of C of circle
 \downarrow \downarrow

$$S = \frac{\frac{1}{3}}{2\pi} \cdot 2\pi(20) = 20\left(\frac{1}{3}\right) = \frac{20}{3} \text{ m.}$$

$$= 6.667 \text{ m}$$

2. $r = 4$ inches, $\theta = 120^\circ$, $s = ?$

$$S = \frac{\frac{120^\circ}{360^\circ}}{3} \cdot 2\pi(4) = \frac{8}{3}\pi'' = 8.378''$$

3. $r = 5$ miles, $s = 2$ miles, $\theta = ?$

$$S = \frac{\theta}{360} \cdot 2\pi r$$

$$2 = \frac{\theta}{360} \cdot 2\pi(5)$$

$$2 = \frac{8\pi}{36}$$

$$72 = 8\pi$$

$$\theta = \frac{72}{\pi}^\circ \approx 22.918^\circ$$

$$S = \frac{\theta}{2\pi} \cdot 2\pi r$$

$$2 = \frac{\theta}{2\pi} \cdot 2\pi(5)$$

$$2 = 5\theta$$

$$\theta = \frac{2}{5} = 0.4$$

$$\theta = 0.4 \text{ radians}$$

A denotes the area of the sector of a circle of radius r formed by the central angle θ . Find the missing quantity. Round answers to three decimal places.

1. $r = 20 \text{ meters}$, $\theta = \frac{1}{3} \text{ radian}$, $A = ?$

$$\begin{aligned} A &= \frac{\text{part of } \theta}{2\pi} \cdot \text{Area of } O \\ &= \frac{1}{3} \cdot \pi(20)^2 = \frac{1}{3} \cdot \pi(400) = \frac{1}{3} \cdot 200\pi \\ A &= \frac{200}{3} \text{ m}^2 \\ A &= 66.667 \text{ m}^2 \end{aligned}$$

2. $r = 4 \text{ inches}$, $\theta = 120^\circ$, $A = ?$

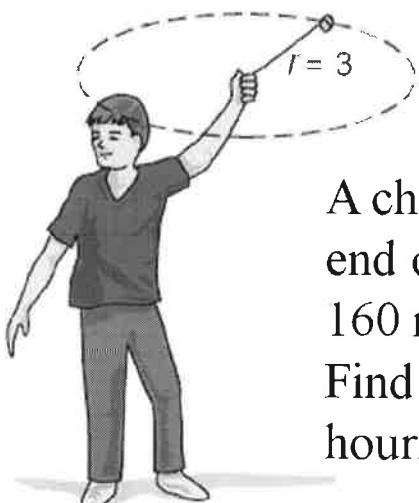
$$\begin{aligned} A &= \frac{120^\circ}{360^\circ} \cdot \pi(4)^2 = \frac{1}{3} \cdot \pi \cdot 16 \\ &= \frac{16}{3}\pi = 16.755 \text{ in}^2 \end{aligned}$$

3. $r = 5 \text{ miles}$, $A = 7 \text{ square miles}$, $\theta = ?$

$$\begin{aligned} A &= \frac{\theta}{2\pi} \cdot \pi r^2 \\ 7 &= \frac{\theta}{2\pi} \cdot \pi(5)^2 \\ 7 &= \frac{25\pi}{2} \theta \end{aligned}$$

$\frac{14}{25} = \theta$
 $\theta = 0.56 \text{ radians}$

Unit Analysis Problem:



$$1 \text{ revolution} = 2\pi(3) = 6\pi \text{ ft.}$$

A child is spinning a rock at the end of a 3-foot rope at the rate of 160 revolutions per minute (rpm). Find how fast is that in miles per hour.

$$\begin{aligned} \frac{160 \text{ rev}}{1 \text{ min}} \cdot \frac{6\pi \text{ ft.}}{1 \text{ rev}} \cdot \frac{1 \text{ mi.}}{5280 \text{ ft.}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} &= \frac{57600\pi \text{ miles}}{5280 \text{ hrs}} \\ &\approx 34.27 \text{ mph} \end{aligned}$$