

1. y varies inversely as x , and $y = 12$ when $x = 4$. Write an equation for the relationship. Find x when $y = 20$.
2. y varies jointly as x and z and inversely as the cube root of w . $y = 1.2$ when $x = 4$, $z = 3$, and $w = 8$. Write an equation for the relationship. Find y when $x = 10$, $z = 4$, and $w = 27$.

Simplify. Give domain restrictions if necessary.

3. $\frac{x+3}{x^2+8x+15}$

4. $\frac{-x^3+x^2}{x^2+x-2}$

5. $\frac{x^2-5x}{x^2-6x+9} - \frac{2}{x-3}$

6. $\frac{4}{x} + \frac{5}{x+2} - \frac{1}{3}$

7. $\frac{x^2-25}{x^3-5x^2+6x} \cdot \frac{x^2-4}{x^2+2x-15}$

8. $\frac{x^2+11x+24}{x+1} \div \frac{x^2+4x+3}{7}$

9. $\frac{x}{x+4} \div \frac{\frac{x^2}{2x+20}}{\frac{x^2+6x+8}{x+10}}$

10. $\frac{2x}{5} \cdot \frac{x^2-16}{4x-12} \cdot \frac{x^2-2x-3}{x^2-3x-4}$

11. $\frac{1}{x} - \frac{5}{6x} + \frac{2}{3}$

Solve each equation. Check your solutions.

12. $\frac{x+2}{x-2} = \frac{x}{-4}$

13. $\frac{x}{x+1} + \frac{2x}{x-1} = \frac{2}{x^2-1}$

14. $5 - \frac{26}{x+2} = \frac{27}{x^2-4}$

15. $\frac{x+5}{x-2} = \frac{28}{x^2-4}$

16. $\frac{x-7}{x+1} - \frac{x-4}{3x-2} = 0$

Answers:

$$1. \ y = \frac{48}{x}; x = 2.4$$

$$2. \ y = \frac{0.2xz}{\sqrt[3]{w}}; y = \frac{8}{3}$$

$$3. \ \frac{1}{x+5}; x \neq -3, -5$$

$$4. \ \frac{-x^2}{x+2}; x \neq -2, 1$$

$$5. \ \frac{x^2-7x+6}{(x-3)^2}; x \neq 3$$

$$6. \ \frac{-x^2+25x+24}{3x(x+2)}; x \neq 0, -2$$

$$7. \ \frac{(x-5)(x+2)}{x(x-3)(x-3)}; x \neq 0, 3, 2, -5$$

$$8. \ \frac{7(x+8)}{(x+1)^2}; x \neq -3, -1$$

$$9. \ \frac{2(x+2)}{x}; x \neq -10, -4, -2, 0$$

$$10. \ \frac{x(x+4)}{10}; x \neq -1, 3, 4$$

$$11. \ \frac{1+4x}{6x}; x \neq 0$$

$$12. \ x = -1 \pm i\sqrt{7}$$

$$13. \ x = \frac{2}{3}$$

$$14. \ x = \{5, \frac{1}{5}\}$$

$$15. \ x = -9$$

$$16. \ x = \{1, 9\}$$