

7.1 Compound Interest Notes

Compound Interest Formula

$$A(t) = P \left(1 + \frac{r}{n} \right)^{nt}$$

annually $n=1$
 semi-annually $n=2$
 monthly $n=12$
 quarterly $n=4$
 weekly $n=52$
 daily $n=365$

P - principal (\$ you invest)

r - annual interest rate (expressed as a decimal)

n - // of time interest is compounded

t - time in years

Ex. 1 Find the final amount of a \$100 investment after 10 years at 5% interest compounded annually, quarterly, and daily.

$A(10) = 100 \left(1 + \frac{0.05}{1} \right)^{(1)(10)} = \162.89 (annually $n=1$)
 $A(10) = 100 \left(1 + \frac{0.05}{4} \right)^{(4)(10)} = \164.36 (quarterly $n=4$)
 $A(10) = 100 \left(1 + \frac{0.05}{365} \right)^{(365)(10)} = \164.87 (daily $n=365$)

Ex. 2 Which will yield more money? Investing \$2000 for 4 years, compounded semi-annually at 3.7% or investing \$1600 for 6 years, compounded weekly at 3.8%?

$A(4) = 2000 \left(1 + \frac{0.037}{2} \right)^{2(4)} = \2315.89
 $A(6) = 1600 \left(1 + \frac{0.038}{52} \right)^{52(6)} = \2009.57

SO yields more money.

Ex. 3 Maria bought a computer for \$1297 five years ago. Unfortunately, it was stolen and her insurance company claims that the value depreciates 14% each year. How much money was her insurance company willing to give her for her stolen computer? "decay"

multiplier $1 - .14 = .86$

$$V = 1297(1 - .14)^5$$

$$= \$610.14$$