

Powers of i

$i^0 = 1$
 $i^1 = i$
 $i^2 = -1$
 $i^3 = -i$
 $i^4 = i^3 \cdot i = -i \cdot i = -i^2 = -(-1) = 1$

$i^5 = i^4 \cdot i = 1 \cdot i = i$
 $i^6 = i^5 \cdot i = i \cdot i = i^2 = -1$
 $i^7 = i^6 \cdot i = -1 \cdot i = -i$
 $i^8 = i^7 \cdot i = -i \cdot i = -i^2 = 1$
 $i^9 = i$
 $i^{10} = -1$
 $i^{11} = -i$
 $i^{12} = 1$

Notice a pattern?

So, how would you find i^{35} ?

$$4 \overline{) 35}$$

$$\underline{32}$$

$$3$$
 remainder

 $i^3 = -i$

Now find i^{99} .
So write pattern

$i^0 = 1$
 $i^1 = i$
 $i^2 = -1$
 $i^3 = -i$

then see where i^{99} is in pattern.

$$4 \overline{) 99}$$

$$\underline{80}$$

$$19$$

$$\underline{16}$$

$3 \leftarrow$ remainder $i^3 = -i$

What would i^{20} be?

$$4 \overline{) 20}$$

$$\underline{20}$$

$$0$$
 remainder

 so $i^0 = 1$

What about i^{21} ?

$$4 \overline{) 21}$$

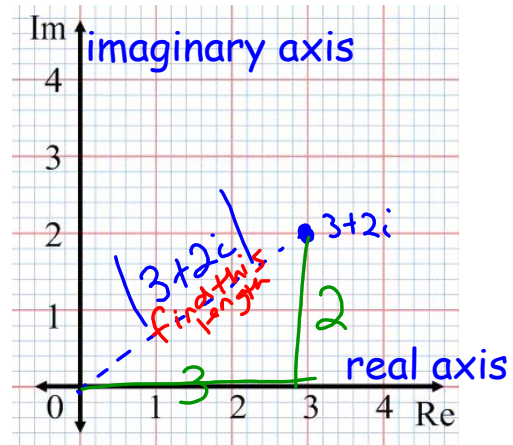
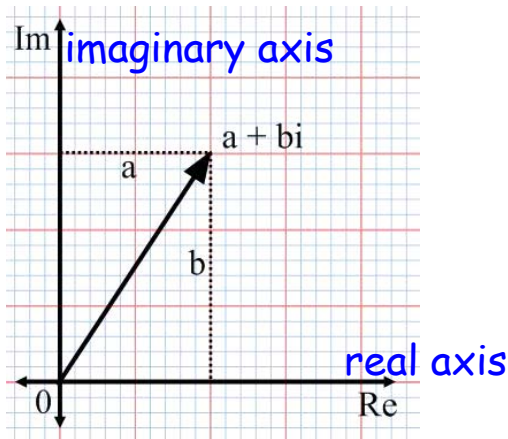
$$\underline{20}$$

$$1$$

 $i^1 = i$

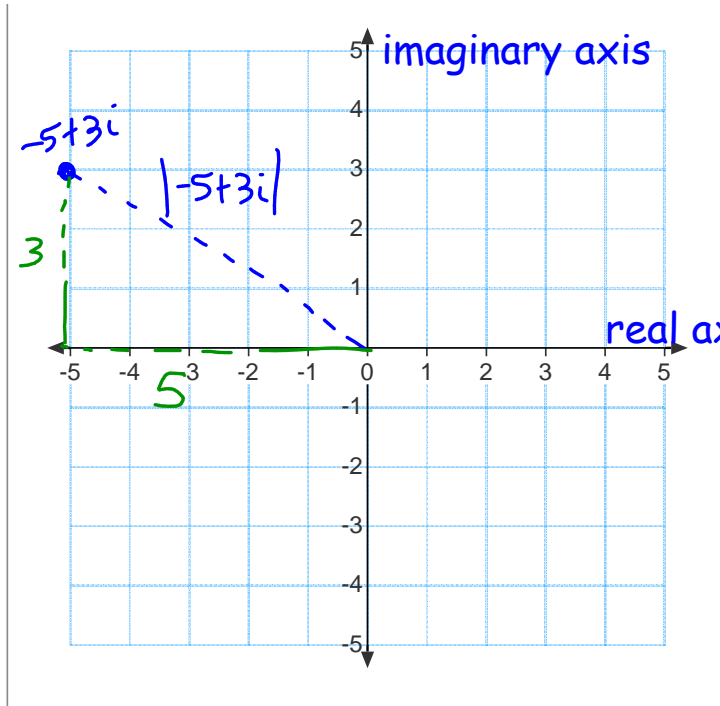
Geometrical Representation of Complex Numbers

A complex number $a + bi$ is represented in the Complex Number Plane as: **EX.**



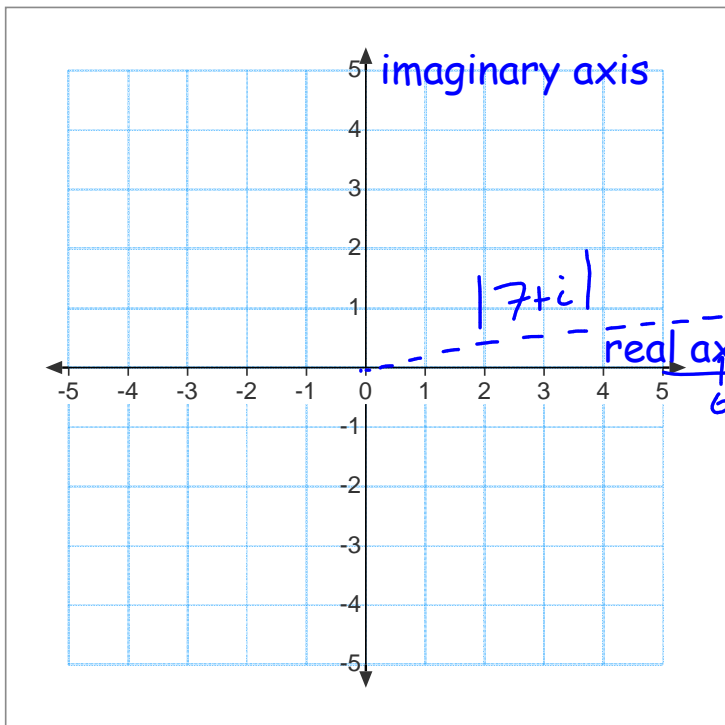
1. Plot the complex number $3 + 2i$ on the Complex Number Plane.
2. Find the absolute value (magnitude) of complex number $3 + 2i$ so $|3 + 2i| = \sqrt{13}$

Use pythag $a^2 + b^2 = c^2$
thru so $c = \sqrt{a^2 + b^2} = \sqrt{3^2 + 2^2} = \sqrt{9 + 4} = \sqrt{13}$



$$\begin{aligned}
 |-5+3i| &= \sqrt{(-5)^2 + (3)^2} \\
 &= \sqrt{25+9} \\
 &= \sqrt{34}
 \end{aligned}$$

1. Plot the complex number $-5 + 3i$ and find its absolute value(MAGNITUDE).



$$\begin{aligned}
 |7+i| &= \sqrt{(7)^2 + (1)^2} \\
 &= \sqrt{49+1} \\
 &= \sqrt{50} \\
 &= \sqrt{25 \cdot 2} \\
 &= 5\sqrt{2}
 \end{aligned}$$

2. Plot the complex number $7+i$ and find its absolute value(MAGNITUDE).