

Solve by the **quadratic formula**.

1. $x^2 + 5x + 6 = 0$

$$x = \frac{-(5) \pm \sqrt{(5)^2 - 4(1)(6)}}{2(1)}$$

$$= \frac{-5 \pm \sqrt{25 - 24}}{2} = \frac{-5 \pm \sqrt{1}}{2}$$

$$= \frac{-5 \pm 1}{2}$$

$$\begin{aligned} \frac{-5+1}{2} &= \frac{-4}{2} = -2 \\ \frac{-5-1}{2} &= \frac{-6}{2} = -3 \end{aligned}$$

3. $x^2 + 7x - 10 = 0$

$$x = \frac{-(7) \pm \sqrt{(7)^2 - 4(1)(-10)}}{2(1)}$$

$$= \frac{-7 \pm \sqrt{49 + 40}}{2} = \frac{-7 \pm \sqrt{89}}{2}$$

2. $x^2 + 6x + 9 = 0$

$$x = \frac{-(6) \pm \sqrt{(6)^2 - 4(1)(9)}}{2(1)}$$

$$= \frac{-6 \pm \sqrt{36 - 36}}{2} = \frac{-6 \pm \sqrt{0}}{2}$$

$$= \frac{-6 \pm 0}{2}$$

$$\begin{aligned} \frac{-6+0}{2} &= \frac{-6}{2} = -3 \\ \frac{-6-0}{2} &= \frac{-6}{2} = -3 \end{aligned}$$

4. $x^2 - 3x + 10 = 0$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(10)}}{2(1)}$$

$$= \frac{3 \pm \sqrt{9 - 40}}{2} = \frac{3 \pm \sqrt{-31}}{2} = \text{non-real solution}$$

Mathematicians invented a new kind of number to deal with situations like #4 on the warm-up.

Since the 1500's $\sqrt{-\#}$ called an **imaginary number**.

In late 1700's Leonard Euler introduced $i = \sqrt{-1}$

So we can simplify the following:

$$1. \sqrt{-4} = \sqrt{-1} \cdot \sqrt{4}$$

$$i(2) = \boxed{2i}$$

$$2. \sqrt{-49} = \sqrt{-1} \cdot \sqrt{49}$$

$$i \cdot 7 = \boxed{7i}$$

$$3. \sqrt{-8} = \sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{2}$$

$$= i \cdot 2 \sqrt{2}$$

$$\boxed{2i\sqrt{2}}$$

And # 4 on the warmup could be completely solved using i.

$$4. x^2 - 3x + 10 = 0$$

$$\begin{aligned} x &= \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(10)}}{2(1)} \\ &= \frac{3 \pm \sqrt{9 - 40}}{2} = \frac{3 \pm \sqrt{-31}}{2} = \frac{3 \pm i\sqrt{31}}{2} \end{aligned}$$

Solve using the quadratic formula. Give exact answers.

$$x^2 + 4x = -5$$

$$x^2 + 4x + 5 = 0$$

$$x = \frac{-4 \pm \sqrt{4^2 - 4(1)(5)}}{2(1)}$$

$$x = \frac{-4 \pm \sqrt{16 - 20}}{2}$$

$$= \frac{-4 \pm \sqrt{-4}}{2} \leftarrow \sqrt{-1} \sqrt{4}$$

$$= \frac{-4 \pm 2i}{2} = \frac{-2 \pm i}{1}$$

$$x = \boxed{-2 \pm i}$$

DISCRIMINANT

The discriminant is:

$$b^2 - 4ac$$

Advanced Algebra 2 - Discriminant Discovery Worksheet

$b^2 - 4ac$ Notice the warmup helps with 1st four

Equation	Value of discriminant	Roots	Description of Roots (Real, Rational, Irrational or Imaginary)	Number of Roots (One double root, two, or two conjugates)
$x^2 + 5x + 6 = 0$	1	-2,-3	real, rational	two
$x^2 - 3x + 10 = 0$	-31	$\frac{3 \pm i\sqrt{31}}{2}$	imaginary	two conjugates
$x^2 + 7x - 10 = 0$	89	$\frac{-7 \pm \sqrt{89}}{2}$	real, irrational	two
$x^2 + 6x + 9 = 0$	0	-3	real, rational	one double root
$3x^2 + 14x - 5 = 0$	256	1/3, -5	real, rational	two
$x^2 - 14x + 34 = -15$	0	7	real, rational	one double root
$(x+2)^2 = 5$	20	$-2 \pm \sqrt{5}$	real, irrational	two
$x^2 - 8x = -31$	-60	$4 \pm i\sqrt{15}$	imaginary	two conjugates
$x^2 + 3x = -1$	5	$\frac{-3 \pm \sqrt{5}}{2}$	real, irrational	two
$(x - 7)^2 = -2$	-8	$7 \pm i\sqrt{2}$	imaginary	two conjugates

How will I know how many REAL solutions exist?

2 REAL solutions? 1 REAL solution? 0 REAL solutions?

2 conjugates

When Given

$$ax^2 + bx + c = 0$$

(discriminant is a positive number)

If $b^2 - 4ac > 0$

then 2 REAL Solutions

-irrational discriminant is not
perfect square
-rational-discriminate
is a perfect square

(discriminant is zero)

If $b^2 - 4ac = 0$

then 1 REAL Solution (double root).

(discriminant is a negative number)

If $b^2 - 4ac < 0$

then 0 REAL Solutions or imaginary- 2 conjugates